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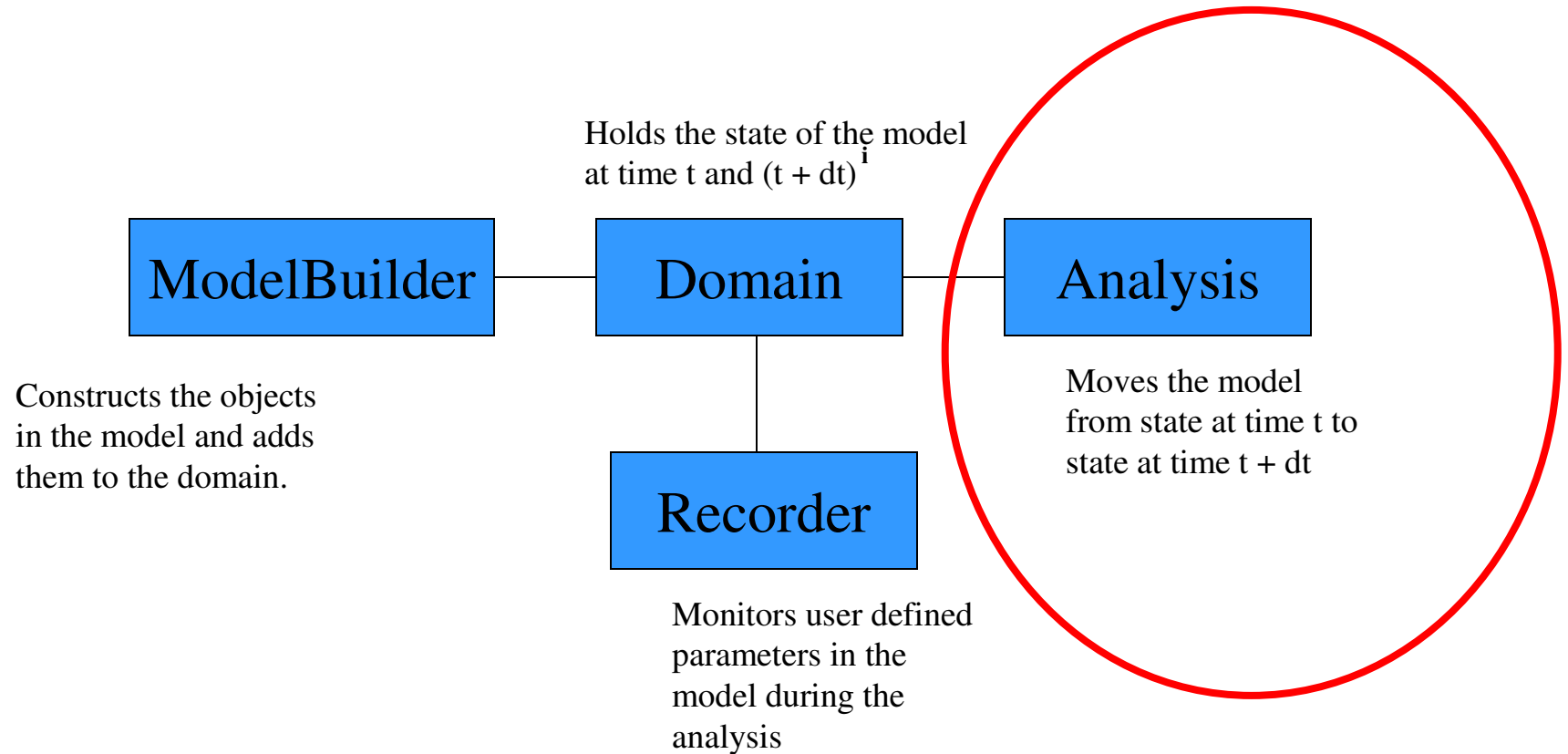
# OpenSees: Analysis

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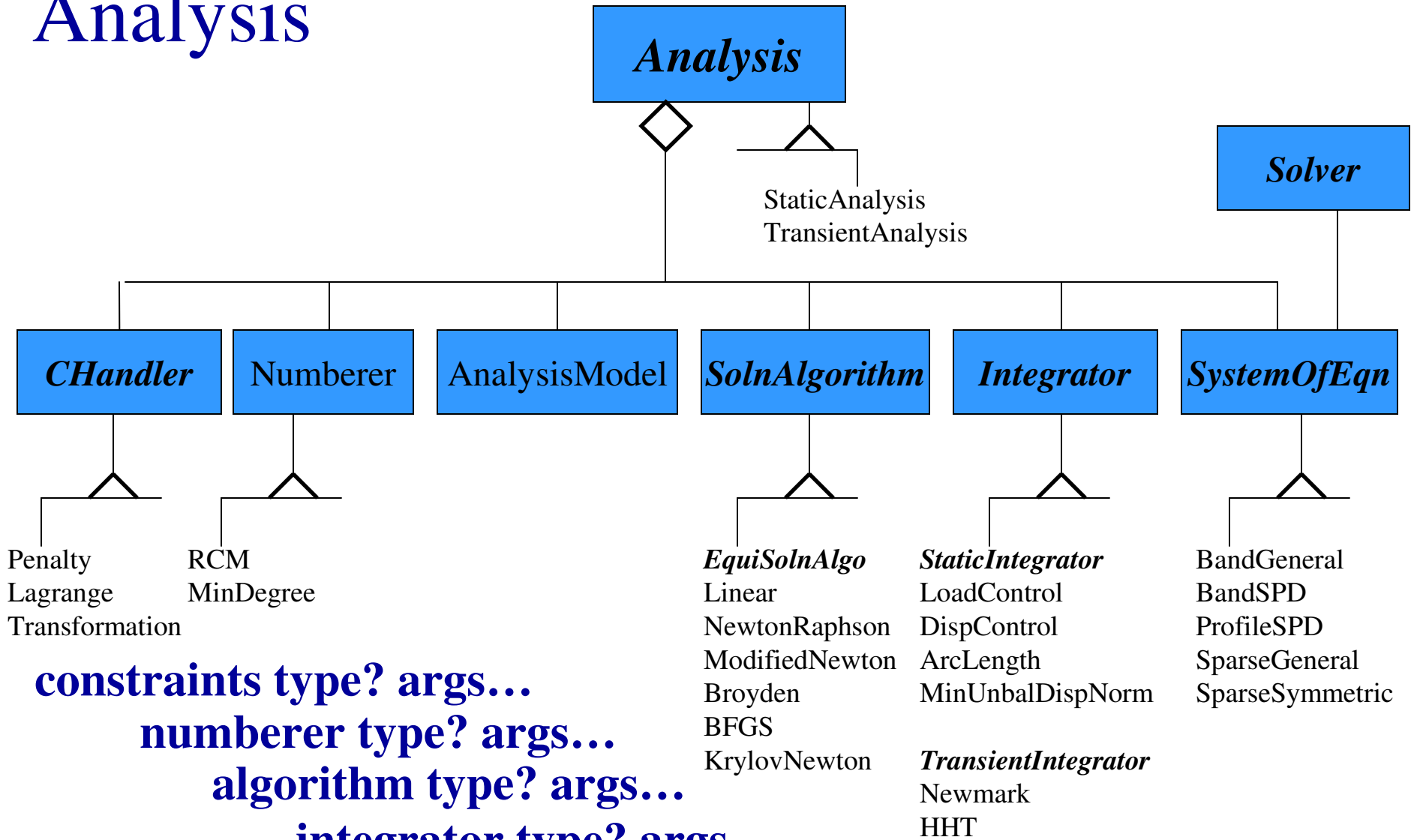


# Main Abstractions in OpenSees



In this presentation we focus on **ANALYSIS GENERATION**

# Analysis



**constraints type? args...**

**numberer type? args...**

**algorithm type? args...**

**integrator type? args...**

**system type? args...**

**analysis type? args...**

**analyze args ...**



# analysis command:

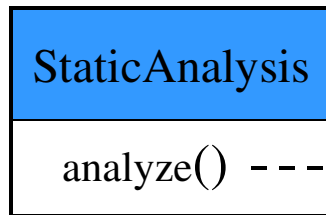
- Static Analysis

*analysis static*

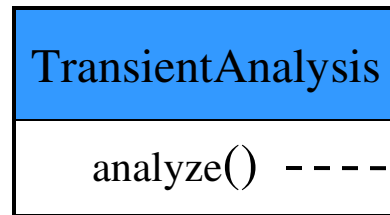
- Transient Analysis

*analysis transient*

- both incremental solution strategies



```
for (int i=0; i<numIncr; i++) {  
  theIntegrator->newStep();  
  theAlgorithm->solveCurrentStep();  
  theModel->commit();  
}
```



```
for (int i=0; i<numIncr; i++) {  
  theIntegrator->newStep(dt);  
  theAlgorithm->solveCurrentStep();  
  theModel->commit();  
}
```

- Eigenvalue

- general eigenvalue problem

$$(\mathbf{K}-\lambda\mathbf{M})\Phi=0$$

*eigen numModes? -general*

- standard eigenvalue problem

$$(\mathbf{K}-\lambda\mathbf{I})\Phi=0$$

*eigen numModes? -standard*

# integrator command:

- determines the predictive step for time  $t+\delta t$
- specifies the tangent matrix and residual vector at any iteration
- determines the corrective step based on  $\Delta U$

## •Transient Integrator for Use in Transient Analysis

Nonlinear equation of the form:

$$\mathbf{R}(\mathbf{U}, \dot{\mathbf{U}}, \ddot{\mathbf{U}}) = \mathbf{P}(t) - \mathbf{F}_I(\ddot{\mathbf{U}}) - \mathbf{F}_R(\mathbf{U}, \dot{\mathbf{U}})$$

### ▪Newmark Method

*integrator Newmark  $\alpha \beta$*

### ▪Hilbert-Hughes-Taylor Method

*integrator Newmark  $\alpha$*

## •Static Integrators for Use in Static Analysis

Nonlinear equation of the form:

$$\mathbf{R}(\mathbf{U}, \lambda) = \lambda \mathbf{P}^* - \mathbf{FR}(\mathbf{U})$$

### ▪Load Control

$$\lambda_n = \lambda_{n-1} + \Delta \lambda$$

*integrator LoadControl  $\Delta \lambda$*

\*does not require a reference load, i.e. loads in load patterns with Linear series and all other loads constant.

### ▪Displacement Control

$$\mathbf{U}_{j_n} = \mathbf{U}_{j_{n-1}} + \Delta \mathbf{U}_j$$

*integrator DisplacementControl node dof  $\Delta \lambda$*

### ▪Arc Length

$$\Delta \mathbf{U}_n^T \Delta \mathbf{U}_n + \alpha^2 \Delta \lambda_n^2 = \Delta s^2$$

*integrator LoadControl  $\alpha \Delta s$*

### ▪Minimum Unbalance Displacement Norm

$$\frac{d}{d\Delta \lambda} (\Delta \mathbf{U}_n^T \Delta \mathbf{U}_n) = \mathbf{0}$$

*integrator LoadControl  $\Delta \lambda$*

# algorithm command:

- to specify the steps taken to solve the nonlinear equation

## •Linear Algorithm

```
theIntegrator->formUnbalance();  
theIntegrator->formTangent();  
theSOE->solve()  
theIntegrator->update(theSOE->getX());
```

```
algorithm Linear
```

## •Newton-Raphson Algorithm

```
theIntegrator->formUnbalance();  
do {  
  theIntegrator->formTangent();  
  theSOE->solve()  
  theIntegrator->update(theSOE->getX());  
  theIntegrator->formUnbalance();  
} while (theTest->test() == fail)
```

```
algorithm Newton
```

## •Modified Newton Algorithm

```
algorithm ModifiedNewton <-initial>
```

## •Accelerated Modified Newton Algorithm

```
algorithm KrylovNewton <-initial>
```

# constraints command:

- to specify how the constraints are enforced

$$\mathbf{U}_c = \mathbf{C}_{rc} \mathbf{U}_r$$

$$\mathbf{C} \mathbf{U} = \mathbf{0}$$

$$\mathbf{T} \mathbf{U}_r = [\mathbf{U}_r \ \mathbf{U}_c]^T$$

$$[\mathbf{C}_r \ \mathbf{C}_c]^T [\mathbf{U}_r \ \mathbf{U}_c] = 0$$

## •Transformation Handler

$$\mathbf{K}^* \mathbf{U}_r = \mathbf{R}^* \quad \mathbf{K}^* = \mathbf{T}^T \mathbf{K} \mathbf{T}$$
$$\mathbf{R}^* = \mathbf{T}^T \mathbf{R}$$

*constraints Transformation*

in OpenSees currently don't allow retained node in one constraint to be a constrained node in another constraint

## •Lagrange Handler

$$\begin{bmatrix} \mathbf{K} & \mathbf{C}^T \\ \mathbf{C} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{U} \\ \boldsymbol{\lambda} \end{bmatrix} = \begin{bmatrix} \mathbf{R} \\ \mathbf{Q} \end{bmatrix}$$

*constraints Lagrange*

## •Penalty Handler

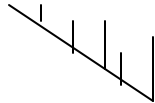
$$[\mathbf{K} + \mathbf{C}^T \alpha \mathbf{C}] \mathbf{U} = [\mathbf{R} + \mathbf{C}^T \alpha \mathbf{Q}]$$

*constraints Penalty  $\alpha_{sp}$ ?  $\alpha_{mp}$ ?*

# system command:

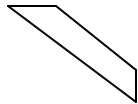
- to specify how matrix equation  $KU = R$  is stored and solved

- Profile Symmetric Positive Definite (SPD)



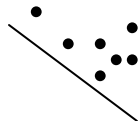
*system ProfileSPD*

- Banded Symmetric Positive Definite



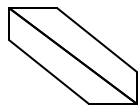
*system BandSPD*

- Sparse Symmetric Positive Definite



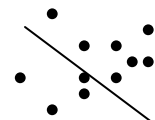
*system SparseSPD*

- Banded General



*system BandGeneral*

- Sparse Symmetric



*system Umfpack*

# numberer command:

- to specify how the degrees of freedom are numbered

- Plain Numberer

nodes are assigned dof arbitrarily

*numberer Plain*

- Plain Numberer

nodes are assigned dof using the  
Reverse Cuthill-McKee algorithm

*numberer RCM*

# test command:

- to specify when convergence has been achieved

all look at system:  $\mathbf{KU} = \mathbf{R}$

- Norm Unbalance

$$\sqrt{\mathbf{R}^T \mathbf{R}} < \mathbf{tol}$$

*test NormUnbalance tol? numIter? <flag?>*

- Norm Displacement Increment

$$\sqrt{\mathbf{U}^T \mathbf{U}} < \mathbf{tol}$$

*test NormDispIncr tol? numIter? <flag?>*

- Norm Energy Increment

$$\frac{1}{2} (\mathbf{U}^T \mathbf{R}) < \mathbf{tol}$$

*test NormEnergyIncr tol? numIter? <flag?>*

- Relative Tests

*test RelativeNormUnbalance tol? numIter? <flag?>*

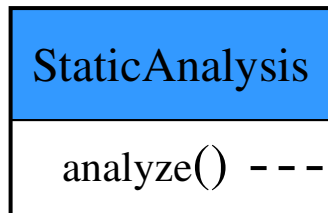
*test RelativeNormDispIncr tol? numIter? <flag?>*

*test RelativeNormEnergyIncr tol? numIter? <flag?>*

# analyze command:

- to perform the static/transient analysis

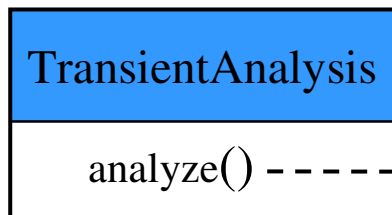
## •Static Analysis



```
for (int i=0; i<numIncr; i++) {  
    theIntegrator->newStep();  
    theAlgorithm->solveCurrentStep();  
    theModel->commit();  
}
```

*analyze numIter?*

## •Transient Analysis



```
for (int i=0; i<numIncr; i++) {  
    theIntegrator->newStep(dt);  
    theAlgorithm->solveCurrentStep();  
    theModel->commit();  
}
```

*analyze numIter?  $\Delta t$ ?*

# Example Analysis:

---

- Static Nonlinear Analysis with LoadControl

```
constraints transformation
numberer RCM
system BandGeneral
test NormDispIncr 1.0e-6 6 2
algorithm Newton
integrator LoadControl 0.1
analysis Static
analyze 10
```

- Transient Nonlinear Analysis with Newmark

```
constraints transformation
numberer RCM
system BandGeneral
test NormDispIncr 1.0e-6 6 2
algorithm Newton
integrator Newmark 0.5 0.25
analysis Transient
analyze 2000 0.01
```

